A GRAPHICAL AID FOR FORECASTING THE CONDITIONAL PROBABILITY OF FREEZING RAIN

JOSEPH R. BOCCHIERI

Techniques Development Laboratory National Weather Service, NOAA Silver Spring, Maryland 20910

ABSTRACT

A graphical aid is developed which gives 12- to 24-hr forecasts of the conditional probability of freezing rain for the conterminous United States. The MOS (Model Output Statistics) concept is used to develop the system. The predictors consist of the 1000-500 mb thickness and boundary layer potential temperature as forecasted by the National Meteorological Center's Limited-Area Fine Mesh (LFM) model. The graphical aid can be used at the local forecast office to supplement the conditonal probability of frozen precipitation (PoF) guidance. The graphical aid is intedned only as an interim technique until a new, more sophisticated, centralized guidance system is developed.

1. Introduction

Since 1 November 1972, an automated system for forecasting the conditional probability of frozen precipitation (PoF) (Bocchieri and Glahn, 1976) has been operational within the National Weather Service (NWS). In the PoF system, "frozen" precipitation is defined as some form of snow or sleet (ice pellets); freezing rain and mixed rain and snow are included with rain and drizzle in the "unfrozen" category. Explicit probability forecasts for the freezing rain event are not available now in the PoF system. Work is continuing on a new, 3-category system in which probability forecasts of snow (and/or sleet), freezing rain, and rain will be given. Mixed precipitation will be included in the rain category. As a result of some preliminary work, a graphical method has been developed that gives 12- to 24-hr forecasts of the conditional probability of freezing rain, the condition being that precipitation occurs. We emphasize that the graphical method should be used at the local forecast office only as an interim technique to supplement the PoF guidance until the new, more sophisticated, centralized guidance system is developed. Therefore, we have not verified the method on dependent or independent data.

As in the PoF system, the Model Output Statistics (MOS) technique (Glahn and Lowry, 1972) was used to develop the graphical aid. The predictors consisted of forecast output from the Limited-Area Fine Mesh (LFM) model (National Weather Service, 1971). In the atmosphere, freezing rain is favored when precipitation falls through a warm upper layer into a shallow, below-freezing surface layer; the upper layer is too warm to support snow or sleet. Therefore, in deriving predictors to help isolate the freezing rain event from other precipitation types, graphs were developed that show the relative frequency of freezing rain as a joint function of the following pairs of LFM predictors, valid at the same time as the precipitation event: 1000-500 mb thickness (10-50 TH) and boundary layer potential temperature (BLPT)', 850-mb temperature and BLPT, 850-500 mb thickness and BLPT, 850-500 mb thickness and 1000-850 mb thickness, and 10-50 TH and 1000-850 mb thickness. Of these pairs, the 10-50 TH and BLPT combination seemed to be the best to isolate the freezing rain event for the developmental data sample.

In a similar approach, Wasserman (1972) developed a graphical method for forecasting the probability of occurrence of four types of precipitation including freezing rain. His predictors were the 10-50 TH and BLPT as forecasted by the Primitive Equation (PE) model (Shuman and Hovermale, 1968). Wasserman's system was designed for use within the Eastern Region of the NWS. The TDL method uses the same predictor variables as Wasserman's, but they are taken from the LFM instead of the PE model; also, the TDL variables can be used at many stations across the conterminous United States. Younkin (1967) related precipitation type to 1000–850 mb thickness and 850–700 mb thickness. However, Younkin used observed thickness values in deriving the relationship; in our method we used the MOS approach.

2. Development

The developmental sample consisted of data combined for 166 stations in the conterminous United States from the winter seasons (September through April) of 1972-73 through 1974-75. The data could be combined from different stations because our predictors, 10-50 TH and BLPT, were in terms of deviations from 50% values. We used the concept of 50% values for our operational PoF system (see Glahn and Bocchieri, 1975). Briefly, a 50% value of a variable is that value at which the conditional probability of frozen precipitation is 50%. The 50% values were computed by using the logit model (Brelsford and Jones, 1967; Jones, 1968) to fit the data. The logit model provides a means of fitting a sigmoid or S-shaped curve when the dependent variable is binary and the independent variable is continuous (see Fig. 2 in Glahn and Bocchieri, 1975). The 50% values vary from station to station mainly due to differences in station elevation. For the LFM model, data from three winter seasons 1972-73 through 1974-75, were used to develop 50% values for 233 MOS stations; these are listed in National Weather Service (1976a).

In developing the graphical method, data were combined not only from different stations, but also from different forecast projections and LFM cycle times. That is, at each station, LFM forecasts of 10–50 TH and BLPT (in terms of deviations from 50% values) and corresponding surface observations of precipitation type for five forecast projections—12-, 15-, 18-, 21-, and 24-hr were matched. The data for all stations and all projections from both the 0000 and 1200 GMT LFM cycle times were then combined into one sample. It was necessary to pool the data to insure that an ample number of freezing rain cases were available. In combining data from different forecasts of 10–50 TH and BLPT did not change with time. This is a reasonable assumption since the time period covered by the projections is only 12 hr.

Next, the relative frequency of freezing rain as a function of 10-50 TH and BLPT for the pooled data sample was computed; only precipitation cases were included in the sample, the results are shown in Fig. 1 in graphical form. The number above each dot is the relative frequency of freezing rain; the number in parentheses below the dot is the number of cases used to com-

¹ The BLPT is the mean potential temperature in the boundary layer of the LFM model. The boundary layer in the LFM model is 50 mb thick, with the bottom of the layer at the earth's surface. The earth's surface is represented in the model by smoothed topography.

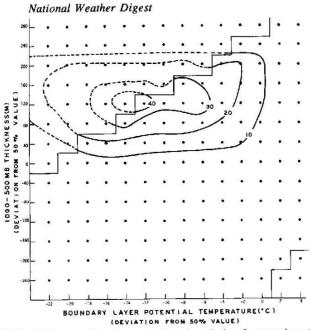
														Noven	mber 1977			
1000-500 MB THICKNESS(M) (Deviation From 50 % value)	280	┢	999	999 •	999	999	999	999	999	0 (1)	20 (5)	8 (13)	0 (13)	0 (16)	0 (30)	0 (148)		
	240	-	999 •	999 •	999 •	999 •	999 •	999 •	999 •	0 • (1)	20 ● (5)	8 • (13)	0 (26)	5 (66)	5 (176)	2 (569)		
	200	L	999 •	999 •	999 •	999 •	999 •	999 •	0 (1)	29 • (7)	10 • (21)	20 (56)	20 (133)	11 • (308)	5 (763)	2 (1854)		
	160	_	999	999 •	999 •	999 •	999 •	33 • (3)	29 (21)	34 • (67)	29 • (111)	27 (215)	20 (485)	11 • (1053)	6 (2159)	3 (4069)		
	120	F	999 •	999 •	0 • (1)	0 • (4)	43 (14)	42 (31)	31 (85)	34 (194)	33 (331)	25 (604)	18 (1249)	11 (2417)	6 (4278)	3 (6388)		
	80	L	999 •	20 • (5)	23 (13)	27 • (22)	33 • (54)	24 • (138)	24 (271)	26 • (506)	24 • (837)	19 • (1437)	14 (2613)	9 (4443)	5 (6796)	3 (7975)		
	40		0 • (7)	10 • (20)	17 (46)	19 (78)	19 • (167)	16 (334)	14 • (590)	13 • (1068)	13 • (1757)	13 • (2855)	10 (4687)	6 (7161)	4 (8568)	3 (7560)		
	0	-	0 • (21)	2 • (66)	6 • (135)	7 • (233)	6 • (401)	7 • (639)	6 • (1071)	5 • (1882)	6 • (3063)	7 • (4574)	6 • (6601)	4 • (8337)	3 • (7503)	2 • (4909)		
	-40	-	0 • (88)	0 • (198)	1 • (346)	2 • (546)	1 • (809)	2 (1220)	3 • (1947)	3 • (3013)	3 • (4528)	3 • (6209)	3 (7338)	3 • (6814)	2 (4428)	2 (2224)		
	-80	-	0 • (212)	0 • (381)	0 • (614)	1 ● (956)	0 • (1335)	1 • (1956)	1 ● (3057)	1 • (4256)	1 • (5618)	1 • (6721)	1 • (6351)] • (4421)	1 • (2209)	1 • (935)		
	-120	_	0 (384)	0 • (635)	0 • (943)	0 ● (1402)	0 • (1874)	0 • (2561)	0 (3727)	1 • (4907)	1 (5776)	0 • (5830)	0 (4549)	0 (2606)	0 (1123)	0 (431)		
	-160	-	0 • (514)	0 • (842)	0 • (1251)	0 ● (1753)	0 • (2282)	0 • (2936)	0 ● (3842)	0 • (4482)	0 • (4522)	0 • (3923)	0 • (2606)	0 • (1208)	0 • (417)	0 ● (141)		
	-200	_	0 (546)	0 (884)	0 • (1358)	0 ● (1818)	0 • (2262)	0 • (2863)	0 (3291)	0 (3042)	0 (2475)	0 (1730)	0 (887)	0 (325)	0 (88)	0 • (23)		
	-249	-	0 (525)	0 (820)	0 • (1205)	0 • (1558)	0 • (1821)	0 • (2114)	0 • (1997)	0 • (1439)	0 • (979)	0 (512)	0 • (193)	0 • (64)	0 • (12)	0 (4)		
			1					1	1	1			1	1		L		
			-22	-20	-18	-16	-14	-12	-10	-8	-6	-4	-2	0	2	4		
				BOU	NDAP	RY L	AYEF	PO	TENT	TIAL	TEN	MPER	ATUR	E (*	C)			
						(D	EVIA	TIO	N FR	OM 5	0 %	ALUE/)					

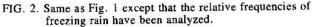
FIG. 1. The empirical probability of freezing rain as a function of 10-50 TH and BLPT. The predictors are forecast values from the LFM model and are given in terms of deviations from 50% values. The graph is valid at any time during the 12- to 24-hr period after the 0000 GMT or 1200 GMT LFM cycle time.

pute the relative frequency. The relative frequencies at each dot were computed from all the cases within a 4°C BLPT interval and an 80 m 10-50 TH interval. For example, in Fig. 1, the relative frequency of freezing rain corresponding to a BLPT deviation of -12° C and a 10-50 TH deviation of +120 m is 42%. This relative frequency was computed from the 31 precipitation cases falling within a -10° C to -14° C BLPT deviation range and a +80 m to +160 m 10-50 TH deviation range. Note that the relative frequencies were computed using overlapping intervals. The solid, jagged line in Fig. 1 separates relative frequencies that were computed with ≥ 25 cases from those which were computed with < 25 cases. A 999 indicates that no precipitation cases were observed for that particular combination of predictor categories. Fig. 2 is similar to Fig. 1, except that the relative frequencies have been analyzed. Note that dashed isopleths are used in the area where the number of cases was judged to be insufficient; the analysis in that area is, of course, questionable.

One can interpret the results shown in Fig. 2 as follows. For 10–50 TH, there is a very small chance of freezing rain when the forecasted *deviation* (from the 50% value) is > 240 m or <

November 1977





0 m. For BLPT, there is a very small chance of freezing rain when the forecasted deviation is > 0°C or < -24°C. The chance of freezing rain is relatively high for a forecasted BLPT deviation near -14°C and a forecasted 10–50 TH deviation near +120 m. In this situation the atmosphere is too warm, in the mean, for the occurrence of snow; but the cold layer near the surface is favorable for the occurrence of freezing rain if precipitation occurs at all.

3. Operational Use

The graph in Fig. 2 can be used at any station that has LFM 50% values for the 10-50 TH and BLPT (National Weather Service, 1976a) and receives LFM forecasts of these variables in real time. The FOUS 60-76 teletypewriter bulletins (National Weather Service, 1976b) provide LFM forecasts of the needed variables. The graph is valid at any time during the 12-24 hr period after the 0000 or 1200 GMT LFM cycle time. It's probably not a good idea to use the graph for other forecast projections since the bias in the predictors may not be the same as the bias for the projections used in development.

A forecaster can use the graph to supplement the early-guidance PoF forecast for a particular station. The PoF gives the conditional probability of occurrence of snow and/or sleet. The forecaster can then get the conditional probability of freezing rain from the graph. Note that the maximum possible conditional probability for freezing rain is about 40%.

Again I must emphasize that the graphical method is considered to be only an interim aid until we can develop a more sophisticated, centralized forecast system. The accuracy of the freezing rain forecasts will probably improve as other predictors and predictor combinations are used.

REFERENCES

- Bocchieri, J. R., and H. R. Glahn, 1976: Verification and Further Development of an Operational Model for Forecasting the Probability of Frozen Precipitation. *Mon. Wea. Rev.*, 104, pp 691–701.
- Brelsford, W. M., and R. H. Jones, 1967: Estimating Probabilities. Mon. Wea. Rev., 95, pp 570-576.

- Glahn, H. R., and D. A. Lowry, 1972: The Use of Model Output Statistics (MOS) in Objective Weather Forecasting. J. Appl. Meteor., 11, pp 1203-1211.
- Glahn, H. R., and J. R. Bocchieri, 1975: Objective Estimation of the Conditional Probability of Frozen Precipitation. Mon. Wea. Rev., 103, pp 3-15.
- Jones, R. H., 1968: A Nonlinear Model for Estimating Probabilities of K Events. Mon. Wea. Rev., 96, pp 383-384.
- National Weather Service, 1971: The Limited-area Fine Mesh (LFM) Model. NWS Tech. Proc. Bull., No. 67, 11 pp.
- National Weather Service, 1976a: Operational Probability of Frozen (PoF) Forecasts Based on Model Output Statistics (MOS). NWS Tech. Proc. Bull., No. 170, 8 pp.
- National Weather Service, 1976b: Realignment of FOUS 60-76 and new FOUS 77 Bulletins. NWS Tech. Proc. Bull., No. 173, 6 pp.
- Shuman, F. G., and J. B. Hovermale, 1968: An Operational six-layer Primitive Equation Model. J. Appl. Meteor., 7, pp 525-547.
- Wasserman, S. E., 1972: Forecasting type of Precipitation. NOAA Tech. Memo. NWS ER-45, 10 pp.
- Younkin, R. J., 1967: A Snow Index. Weather Bureau National Meteorological Center Tech. Memo. WBTM NMC-40, 5 pp.

WEATHER SERVICES CORPORATION

131A GREAT ROAD, BEDFORD, MASS. 01730

JOHN E. WALLACE PETER R. LEAVITT JOHN P. MURPHY

CERTIFIED CONSULTING METEOROLOGISTS

- Worldwide Operational Forecasts
- Agricultural Services
- Offshore Weather and Sea State Forecasting Services
- Environmental Meteorology
- Forensic Meteorology and Expert Testimony
- Climatological Studies
- Radio and Television News Services

Telephones:

Bedford, Mass (617) 275-8860 New York, N.Y. (212) 267-1500 Minneapolis, Minn. (612) 338-3900 Twx (710) 326-0799 Telex 92-3330